

A Centrosymmetric Hexagonal Magnet with Superstable Biskyrmion Magnetic Nanodomains in a Wide Temperature Range of 100–340 K

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Magnetic skyrmions are topologically protected vortex-like nanometric spin textures that have recently received growingly attention for their potential applications in future high-performance spintronic devices. Such unique magnetic nanodomains have been recently discovered in bulk chiral magnetic materials, such as MnSi,^[1–4] FeGe,^[5,6] FeCoSi,^[7] Cu₂OSeO₃,^[8–10] β -Mn-type Co-Zn-Mn,^[11] and also GaV₄S₈,^[12] a polar magnet. The crystal structure of these materials is cubic and lack of centrosymmetry, leading to the existence of Dzyaloshinskii–Moriya (D–M) interactions. Unlike the conventional spin configurations, such as helical or conical, that are usually found in chiral magnets, a magnetic skyrmion has a particle-like swirling-spin configuration characterized by a topological index called the skyrmion number.^[13,14] The nontrivial topology of magnetic skyrmions results in a number of intriguing electromagnetic phenomena, including the topological Hall effect,^[2] skyrmion magnetic resonance,^[15] and thermally induced ratchet motion.^[16] These topologically protected properties, together with their nanoscale dimensions (10–100 nm) and ultralow threshold for current-driven motion (10^5 – 10^6 A m⁻²),^[17–19] make the magnetic skyrmions promising materials for technological applications in spintronic devices.^[20]

In addition to the observation of magnetic skyrmions in chiral magnets characterized by D–M interactions, magnetic skyrmions have also been recently identified in centrosymmetric magnets with uniaxial magnetic anisotropy.^[21] In particular, magnetic biskyrmions (or skyrmion molecules), a new type of skyrmion formed by two skyrmions of opposite spin helicities, have been found in a centrosymmetric bilayered magnetite.^[22] Compared with a single skyrmion in cubic chiral-lattice magnets, a unique feature of such biskyrmions is that their topological charges and sizes can be controlled by the thickness of the sample, the external magnetic field, and even the electrical current, which render them promising materials for alternative information storage media in spintronics applications. However, experimental observations of biskyrmions have, thus far, been limited to bilayered magnetites at temperatures below 60 K, making their use in room temperature (RT) spintronic devices impracticable. Finding new materials that host magnetic biskyrmions at RT is thus crucial to their further development and use.

One possible path to the discovery of new centrosymmetric magnets that can host skyrmions near RT is to revisit noncubic, noncollinear magnets that have been reported to be ferromagnetic above RT. As in bilayered magnetite,^[22] the magnetic dipolar interaction combined with the low crystal symmetry in such magnets might provide additional stability to skyrmions. In what follows, we describe a hexagonal magnet, MnNiGa, that has a layered Ni₂In-type structure^[23] (space group *P63/mmc*) with alternating stacks of Mn atomic layers and Ni-Ga atomic layers along the *c*-axis (Figure 1a). In our previous work,^[24] we have established a stable magnetic–structural coupling and realized a giant magnetocaloric effect in another Ni₂In-type hexagonal MnNiGe:Fe compounds. Moreover, we have fabricated the off-stoichiometry sputtered MnNiGa hexagonal film, which showed some abnormal transport properties.^[25] For the Ni₂In-type MnNiGa compound, the 2(a) site is preferentially occupied by Mn atoms, while the 2(d) is mainly occupied by Ni atoms, in off-stoichiometric cases, extra Mn atoms can also occupy this site, and the 2(c) site is occupied by Ga atoms. Previous powder neutron diffraction experiments^[26] revealed that the magnetic structure varies with the Mn concentration, causing the spin-orientation to shift with changing temperature.

Here, we report on the experimental discovery of biskyrmion magnetic nanodomains at RT and the observation of a biskyrmion-derived topological Hall effect (THE) in the

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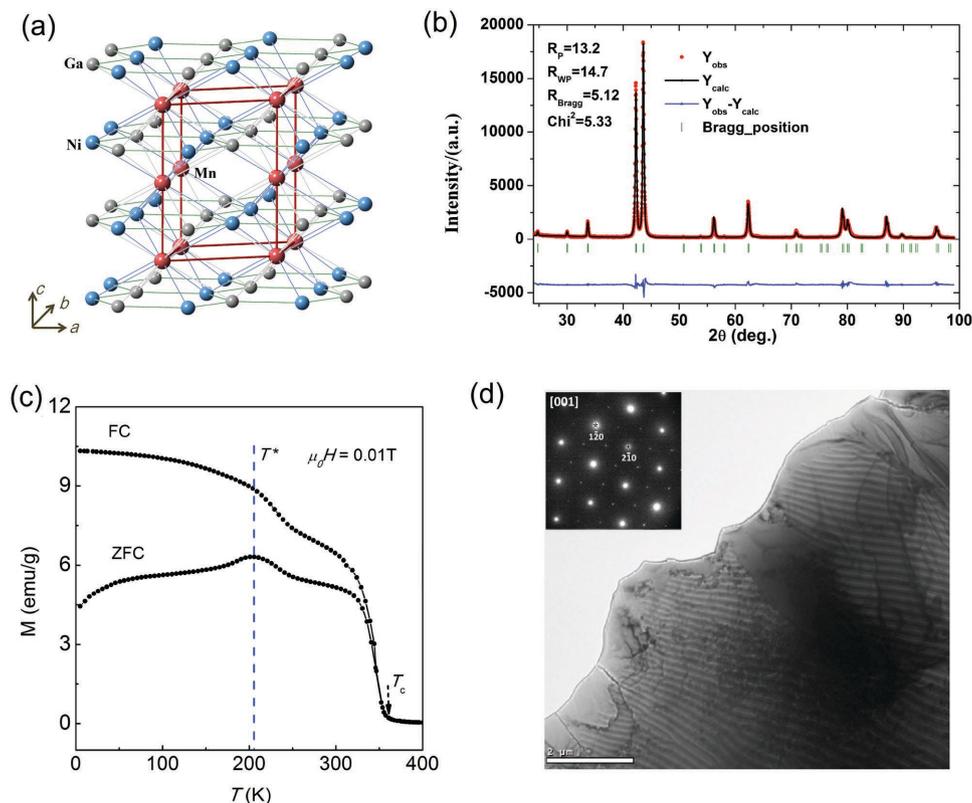


Figure 1. Structural and magnetic properties of $(\text{Mn}_{1-x}\text{Ni}_x)_{65}\text{Ga}_{35}$ with $x = 0.5$. a) Schematic of a layered Ni_2In -type structure Mn-Ni-Ga (space group $P63/mmc$) with alternating stacks of Mn atomic layers and Ni-Ga atomic layers along the c -axis. b) The Rietveld refinement of the powder X-ray diffraction pattern of the sample. c) Temperature dependence of the zero-field cooling (ZFC) and field-cooling (FC) magnetization curves measured at $\mu_0H = 0.01$ T. d) The Lorentz TEM image taken at room temperature shows the uniform magnetic stripe. The scale bar is $2 \mu\text{m}$. The inset shows the selected area electron diffraction (SAED), which indicates the $[001]$ orientation.

centrosymmetric hexagonal MnNiGa magnet. Using a phase reconstruction technique based on a transport-of-intensity equation (TIE), we established the texture of the biskymion spin. Results from Lorentz transmission electron microscopy (TEM) and the topological Hall effect revealed that the biskymion phase is stable over a much wider temperature range (100–340 K) and a larger magnetic field range in our material than in skyrmion-hosting bulk crystals reported previously.^[1–3,6] The super-wide operating temperature and the broad range of material options indicate important progress toward the realization of skyrmion-based spintronic devices.

We synthesized a series of polycrystalline $(\text{Mn}_{1-x}\text{Ni}_x)_{65}\text{Ga}_{35}$ ($0.15 \leq x \leq 0.5$) alloys by induction melting pure metals in an argon atmosphere (see the Experimental Section). Powder X-ray diffraction measurements and Rietveld refinements indicated that all as-prepared samples crystallized into an Ni_2In -type structure. Upon substituting Ni with Mn, the c -axis increased and the a -axis decreased (Figure S1, Supporting Information). The Curie temperature, T_c , systematically decreased with increasing x with a minimum at $x = 0.2$, which is consistent with the results reported by Shiraishi et al.^[26] Uniform magnetic stripe structures are observed in most $(\text{Mn}_{1-x}\text{Ni}_x)_{65}\text{Ga}_{35}$ ($0.15 \leq x \leq 0.5$) alloys (Figure S2, Supporting Information). In the present study, we focus only on the $(\text{Mn}_{1-x}\text{Ni}_x)_{65}\text{Ga}_{35}$ alloy with $x = 0.5$, since it has the highest T_c at ≈ 350 K with a shorter stripe periodicity (Figure 1c,d). According to previous

powder neutron diffraction measurements in off-stoichiometric MnNiGa (ref. [26]), the Mn spin arrangement at the 2(a) site is a canted one, with ferromagnetic components parallel to the c -axis. Thus, the canting of the two Mn spins toward the c -axis is considered to be the origin of the weak magnetic anisotropy in this material system. Moreover, as shown in Figure 1c, a hump is observed at temperature $T^* \approx 200$ K, which indicates the appearance of a new magnetic structure but remain a topic for future investigations.

Figure 2 shows under-focused Lorentz TEM images of revolving skyrmions with different magnetic fields in $(\text{Mn}_{1-x}\text{Ni}_x)_{65}\text{Ga}_{35}$ alloy with $x = 0.5$ measured at $T = 300$ K. At $\mu_0H = 0$ T (Figure 2a), a spontaneous magnetic stripe structure with a periodicity of $\lambda \approx 180$ nm is observed. In Figure 2b, we present the corresponding spin texture obtained by using the TIE. The green and red regions shown in Figure 2b correspond to in-plane anti-parallel magnetic domains, while the black regions represent the out-of plane magnetic domains. The revolving behavior of the biskymions under a vertical magnetic field is similar to that reported previously.^[5,7,8,21,22] The dynamics of formation and disappearance of the biskymions with increasing applied magnetic field were successfully recorded by using in situ Lorentz TEM (see Movie S1, Supporting Information). The threshold magnetic field of skyrmion formation depends on the sample thickness and the temperature. With increasing magnetic field, the magnetic stripes

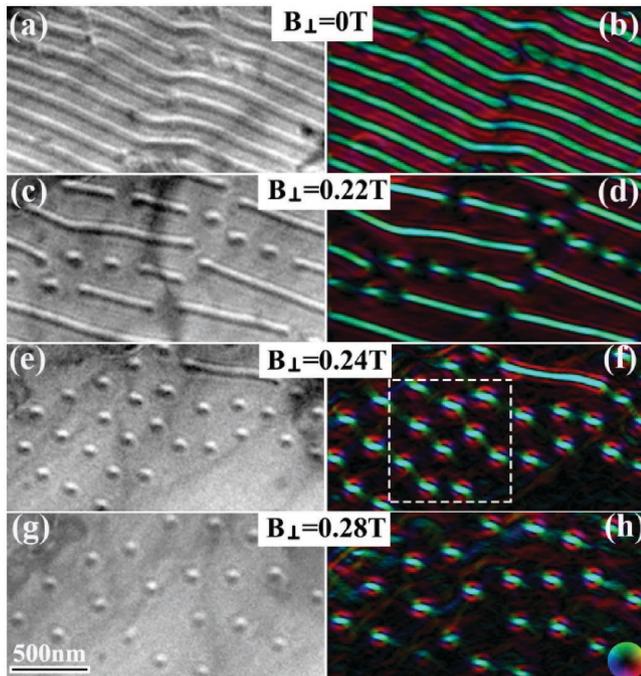


Figure 2. Magnetic field dependence of biskyrmions in real-space Lorentz TEM images at room temperature. a) The under-focused Lorentz TEM image of in-plane spontaneous stripes taken at zero field and b) the corresponding spin texture obtained by TIE analysis of the Lorentz TEM data. c) Under-focused Lorentz TEM images of broken stripes and biskyrmions at a magnetic field of 0.22 T applied normal to the plane. e) Lorentz TEM images (under-focused) of dominant biskyrmions at a larger magnetic field of 0.24 T. g) Under-focused Lorentz TEM images of a completely biskyrmion state when the perpendicular magnetic field is increased to 0.28 T. d, f, h) Corresponding in-plane magnetization distribution maps obtained by the QPt software based on the transport of intensity equation (TIE). The colors and arrows depict the magnitude and orientation of in-plane magnetizations. The color wheel is in the right corner. The scale bar is 500 nm.

narrow first and then break into fragments at the locations where the stripes narrow faster (Figure 2c–f). Simultaneously, the biskyrmions domains begin to appear. As the magnetic field increases further to 0.28 T (Figure 2g, h), the magnetic stripes are completely replaced by individual biskyrmions domains. When the magnetic field is stronger than 0.3 T, the size of the biskyrmions domains begins to shrink and they eventually vanish at a critical magnetic field of 0.4 T. This critical magnetic field is likely a function of the temperature and sample thickness, closely correlated to the saturation magnetic field at which a uniform ferromagnetic domain is formed.

Figure 3 shows part of magnified images of Figure 2e. The opposite magnetic contrast between the under-focused (Figure 3a) and over-focused (Figure 3b) Lorentz TEM images of the biskyrmions is clearly different from the contrast observed in traditional skyrmions with $N_s = 1$. Figure 3c shows the corresponding spin textures of the highlighted area in Figure 2f obtained by TIE analyses of the Lorentz TEM data. To reveal the spin texture of biskyrmions, we show magnified, over-focused and under-focused Lorentz TEM images of a biskyrmion in Figure 3e, f, respectively. The corresponding TIE analysis (Figure 3d) clearly indicates that each spin configuration is composed of two single skyrmions with opposite magnetic helicities; that is, each skyrmion has clockwise (CW) and counter-clockwise (CCW) spin curls with an out-of-plane magnetization culminating at the core. This spin configuration is the same as that of biskyrmions reported by Yu et al.^[22] with $N_s = 2$. We define the polarity of constituent skyrmions as plus (+) for CW skyrmions and minus (–) for CCW skyrmions. The formation of biskyrmions stems from the helicity degree of freedom (+ or –) of each skyrmion, which can be realized only in centrosymmetric magnets and not in chiral-lattice magnets with D–M interactions. However, in contrast with the random polarity of skyrmions observed in another centrosymmetric magnet,^[21] the polar direction of the biskyrmion described here is fixed in MnNiGa, which agrees well with previous observations in bilayered magnetites.^[22]

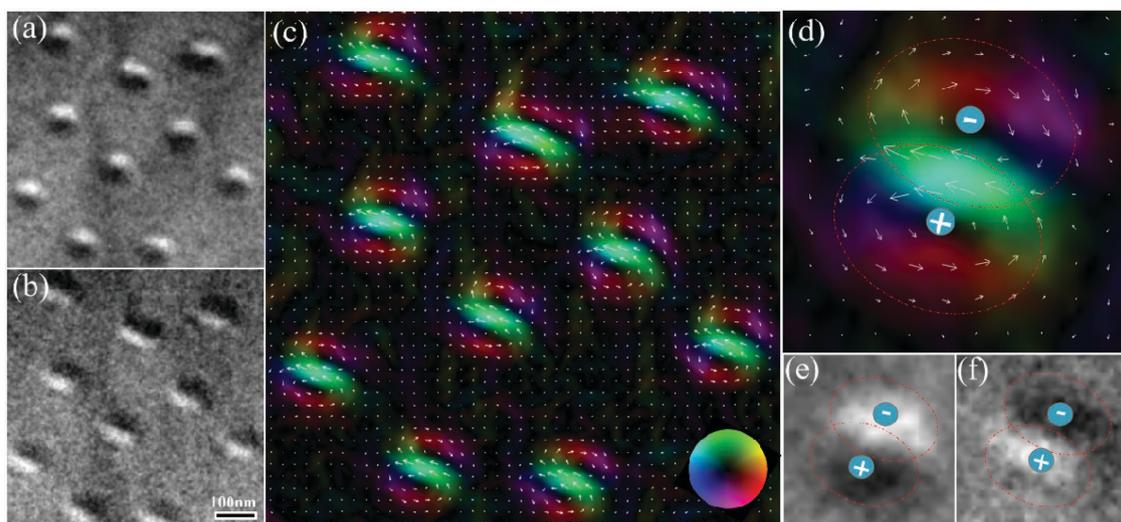


Figure 3. Magnetic configurations of the biskyrmions. a) Under-focused and b) over-focused images of the biskyrmions. c) The corresponding in-plane magnetization distribution map with a color wheel in the inset. d) An enlarged single biskyrmion showing the in-plane, vortex-like spin configuration. e) Under-focused and f) over-focused Lorentz TEM image of a single biskyrmion. The scale bar is 100 nm. In (d)–(f), plus (+) and minus (–) indicate the magnetic helicity; that is, the clockwise- and counter-clockwise rotating directions of in-plane magnetizations around the core, respectively.

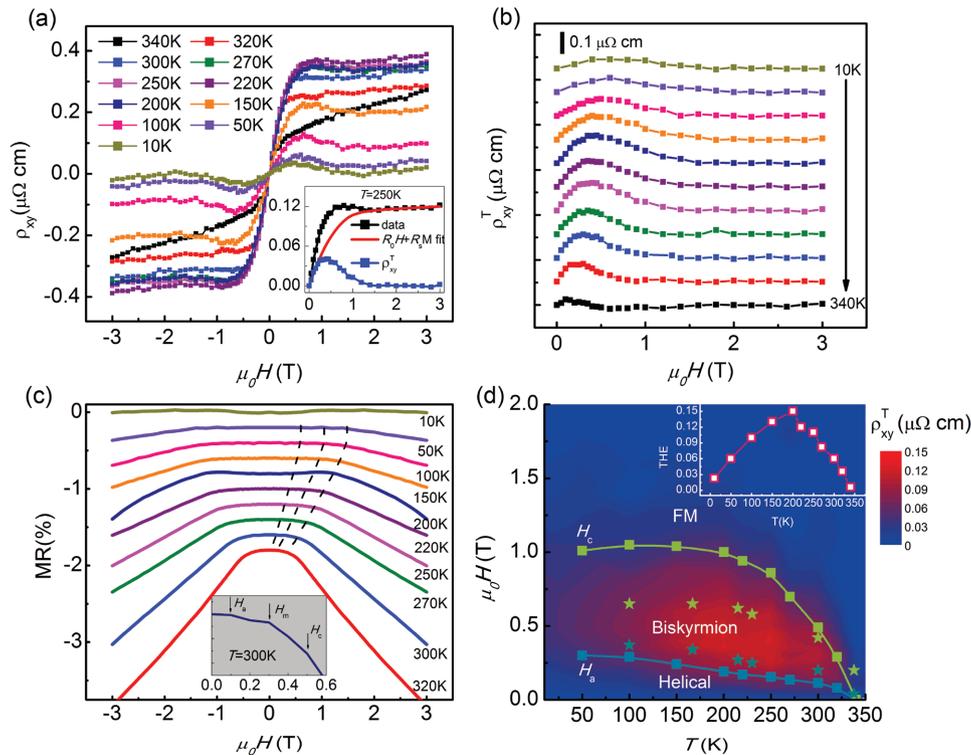


Figure 4. Topological Hall effect, magnetoresistivity, and corresponding magnetic phase diagrams. a) Hall resistivity (ρ_{xy}) measured at various temperatures from 10 to 340 K. Inset (a): The representative ρ_{xy} - H curve (black line) measured at 250 K, calculated $R_0H + R_S M$ curve (red line), and derived ρ_{xy}^T curve (blue line) from the analysis. At high magnetic fields, the calculated result is in accord with the experimental curve. b) Topological resistivity (ρ_{xy}^T) at various temperatures extracted from ρ_{xy} - T curves in (a). c) Normalized magnetoresistivity measured from 10 to 320 K. The dashed lines indicate the approximate positions of the critical field corresponding to the H_a (blue line) and H_c (yellow line) in the H - T phase diagram in panel (d). d) The contour mapping of extracted ρ_{xy}^T as a function of the external magnetic field (H) and temperature (T) for MnNiGa; The blue and yellow lines are the values of H_a and H_c , which indicate the phase boundaries between the helical, biskymion, and field-induced spin collinear FM states. The blue and yellow stars indicate the experimental data based on the in situ Lorentz TEM observations. Inset of (d): maximum values of ρ_{xy}^T as a function of temperature.

In addition to direct observations from Lorentz TEM, magnetic transport measurements, especially observations of the THE, have been considered as a hallmark for the existence of the spin chirality, e.g., the skyrmion spin textures in helimagnets with B20 crystal structure.^[2,27–30] In **Figure 4a**, we show the Hall resistivities ρ_{xy} , measured at various temperatures from 340 to 10 K. In the presence of a topological spin texture, the total Hall resistivity can usually be expressed as the sum of various contributions: $\rho_{xy} = R_0H + R_S M + \rho_{xy}^T$, where R_0 is the ordinary Hall coefficient, R_S is the anomalous Hall coefficient, ρ_{xy}^T is the topological Hall resistivity as possible induced by the biskymion spin textures, H is magnetic field perpendicular to the sample plane, and M is the corresponding magnetization. To extract THE quantitatively, we singled out both the ordinary and anomalous Hall resistivities from ρ_{xy} . As shown in **Figure 4c**, the perpendicular magnetoresistance is very small (less than 3%) and R_S is nearly constant with a magnetic field. Therefore, as in previous studies,^[29] R_S can simply be determined from $R_S = S_A \rho_{xx}^2$, where S_A is independent of the magnetic field. Here, we define the kink field as the critical field H_c . At high fields ($H > H_c$), ρ_{xy}^T is supposed to be zero because all spins are aligned. Hence, combining with field-dependent magnetization $M(H)$ curves measured at different temperatures (**Figure S3**, Supporting Information), we determine the R_0 and

S_A from the intercept and the slope of the linear fitting of ρ_{xy}/H versus $\rho_{xx}^2 M/H$ in high magnetic field regions (**Figure S4**, Supporting Information). We can thus extract ρ_{xy}^T from the difference between the total Hall resistivity ρ_{xy} and the fitted curve $R_0H + R_S M$ at $H < H_c$. In the inset of **Figure 4a**, we show the representative ρ_{xy} - H curve (black line) measured at 250 K, calculated $R_0H + R_S M$ curve (red line) and the derived ρ_{xy}^T curve (blue line) from the analysis. At $H > H_c$, the calculated result is in accord with the experimental data (**Figure S5**, Supporting Information). Strikingly, a hump-like maximum in the curves of ρ_{xy}^T as a function of the applied magnetic field is evident, which was assumed to be a unique signature of THE.^[2,28,30] The ρ_{xy}^T values obtained from the experimental data measured over the temperature range of 10–350 K are shown in **Figure 4b**, where a sizable ρ_{xy}^T is clearly found over the whole temperature range. We note that R_0 is positive at all temperatures, indicating hole-like conduction in MnNiGa. However, the sign of R_S is positive at high temperatures and changes to negative at temperatures below 100 K.

Furthermore, the perpendicular magnetoresistance data measured over a broad temperature range (10–340 K) in the MnNiGa alloy shows three apparent kinks (highlighted by dashed lines in **Figure 4c**), indicative of three critical magnetic fields, identified as H_a , the transition field from the helical to

the biskyrmion state, H_m , the magnetic field of the pure biskyrmion state, and H_c , the transition field from the biskyrmion to the full ferromagnetic state. These critical magnetic fields were previously identified in magnetoresistance curves of bulk MnSi³¹ and nanowire samples.^[19,33]

Based on the temperature-dependent Lorentz TEM images (Figure S6 and Table S1, Supporting Information), magnetoresistance data, and Hall effect results obtained from MnNiGa thin plates, we created biskyrmion phase diagrams (Figure 4d) as represented by contour mapping of the derived ρ_{xy}^T value in the temperature (T) and magnetic field (H) planes. The biskyrmion phase indicated by the emergence of the THE extends across a broad region in the T - H plane, spanning from 340 to nearly 50 K and occupying almost all the region below H_c except the near-zero magnetic field. Within such a broad temperature range, as shown in inset of Figure 4d, the sign of ρ_{xy}^T is positive and varies systematically and reaches a maximum value of $\rho_{xy}^T \approx 0.15 \mu\Omega \text{ cm}$ in the vicinity of 200 K. This result is consistent with the temperature dependence we observed in the Lorentz TEM images, as shown in Figure S6 (Supporting Information), in which the biskyrmion density is roughly at a maximum at $T = 215 \text{ K}$. This maximum value of the observed ρ_{xy}^T ($\approx 0.15 \mu\Omega \text{ cm}$) for MnNiGa is almost same as that for bulk MnGe ($\approx 0.16 \mu\Omega \text{ cm}$),^[31] which has a largest ρ_{xy}^T value among the bulk B20-type chiral magnets. The THE resistivity resulting from the fictitious magnetic field generated by the skyrmion spin textures can be approximated with $\rho_{xy}^T \approx PR_0 B_{\text{eff}}^z$,^[2] where B_{eff}^z is the fictitious effective field and P is the local spin polarization of the charge carriers. Our band structure calculations indicated that the net spin polarization at the Fermi surface is around 0.33 for $(\text{Mn}_{1-x}\text{Ni}_x)_{65}\text{Ga}_{35}$ with $x = 0.5$ (Figure S7, Supporting Information). For MnNiGa, the estimated B_{eff}^z is about 1.1 T if we take the biskyrmion size as 90 nm with topological number of 2.^[29] Taking into account the value of $R_0 = 0.036 \mu\Omega \text{ cm T}^{-1}$ measured at $T = 340 \text{ K}$ for MnNiGa, we obtained a value of $\rho_{xy}^T \approx 0.012 \mu\Omega \text{ cm}$. This value is in good agreement with the experimental value of $0.01 \mu\Omega \text{ cm}$. But with lowering temperature, the value of THE dramatically increases and reaches a maximum value of $0.15 \mu\Omega \text{ cm}$ at $T = 200 \text{ K}$. This inconsistency may be originated from the new spin texture appearing at temperatures around 200 K as we mentioned above, which can cause potential error for extracting THE signal.

The formation of biskyrmion magnetic nanodomains in a hexagonal $(\text{Mn}_{1-x}\text{Ni}_x)_{65}\text{Ga}_{35}$ with $x = 0.5$ magnet was clearly demonstrated by direct real-space Lorentz TEM observations and confirmed indirectly by THE. In striking contrast to other skyrmion-hosting crystals in which magnetic skyrmion nanodomains are stable only in a narrow temperature range, as shown in Figure 5, the biskyrmion states in MnNiGa are stabilized over an extremely wide temperature and magnetic field range. In addition, our discovery suggests that a potentially huge family of non-cubic, centrosymmetric crystals will lead to deeper exploration of novel skyrmion-hosting materials. The very broad temperature range and magnetic field range in which the biskyrmions stably existed are extremely important for both fundamental research and potential applications in novel spintronic devices. The stability of skyrmion lattices over extended areas in their ground state at room temperature has been observed in patterned ultrathin single-layer and multilayer

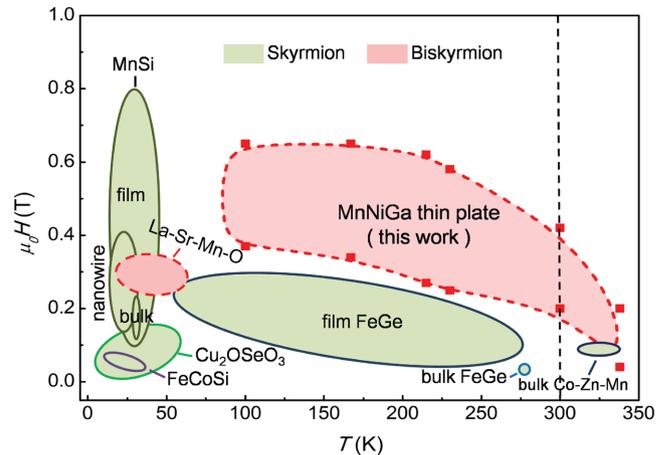


Figure 5. Comparison of the region of skyrmion formation in temperature-magnetic field (T - H) plane for the magnetic skyrmion- and biskyrmion-hosting materials, respectively. Films and nanowires are also included for reference. The data are taken from the open literatures, including refs. [1–12,22,29–31] and [33]. The red solid squares indicate the experimental data based on the in situ Lorentz TEM observations.

magnetic films with perpendicular magnetic anisotropy.^[34–38] In these systems, both the “intrinsic” interfacial D–M interactions and the defect-related “extrinsic” factors (e.g., edge defects and surface roughness) played important roles in inducing magnetic vortex states. More theoretical studies are needed to determine if the biskyrmion phase originated from the magnetic dipolar interaction or other unknown mechanisms related to the defects. To address this issue, further small-angle neutron scattering (SANS) experiments are needed to shed light on the bulk nature of the magnetic structures of MnNiGa with varying compositions. Since such a topological spin structure can be realized in polycrystalline materials in an extremely wide temperature range, our findings not only open up a new pathway for further experimental and theoretical studies of quantum magneto-transport properties, e.g., the quantum Hall effect and topological Hall effect, but they may also lead to the realization of skyrmion-based spintronic devices.

Experimental Section

Sample Preparation: A series of polycrystalline $(\text{Mn}_{1-x}\text{Ni}_x)_{65}\text{Ga}_{35}$ ($0.15 \leq x \leq 0.5$) alloys were synthesized by arc-melting mixtures of highly pure Mn, Ni, and Ga metals in a pure argon atmosphere. Excess Mn (2 mol%) over the stoichiometric composition was added to compensate for loss during arc-melting. The crystal structure of the alloys was studied using powder X-ray diffraction measurements and lattice constants were calculated using Rietveld refinements. The composition was analyzed by both energy dispersive X-ray analysis installed in a scanning electron microscopy and inductively coupled plasma spectroscopy.

Magnetic and Transport Measurements: To measure the (magneto-) transport properties, several polycrystalline crystals were milled into a bar-shape with a typical size of about $3.0 \times 1.0 \times 0.05 \text{ mm}^3$. Both longitudinal and Hall resistivities were measured using a standard four-probe method on a Quantum Design Physical Property Measurement System (PPMS). The field dependence of the Hall resistivity was obtained after subtracting the longitudinal resistivity component. The zero-field remnant magnetization, M , was also measured using the

same field-cooling procedures as used in both longitudinal and Hall resistivity measurements using the Quantum Design PPMS.

Lorentz TEM Measurements: The thin plates for Lorentz TEM observations were cut from bulk polycrystalline samples and thinned by mechanical polishing and argon-ion milling. The magnetic domain contrast was observed by using Tecnai F20 in the Lorentz TEM mode and a JEOL-dedicated Lorentz TEM, both equipped with liquid-nitrogen, low-temperature holders (≈ 100 K) to study the temperature dependence of the magnetic textures. The magnetic structures could be examined directly in the electron microscope by making use of the Lorentz force experienced by a beam of electrons traversing a magnetic field. The Lorentz TEM is very powerful for observing magnetic configurations in ferromagnetic materials owing to its high spatial resolution. To determine the spin helicity of the skyrmions, the three sets of images with under-, over-, and just (or zero) focal lengths were recorded by a charge coupled device (CCD) camera and then the high-resolution in-plane magnetization distribution map was obtained by the QPT software based on the TIE. The inversion of magnetic contrast can be seen between the under- and over-focused images. The colors and arrows depict the magnitude and orientation of the in-plane magnetization. The objective lens was turned off when the sample holder was inserted and the perpendicular magnetic field was induced to the stripe domain by increasing the objective lens in small increments. The specimens for the TEM observations were prepared by polishing, dimpling, and subsequently ion milling. The grain size was large enough to be treated as a single grain in TEM. The crystalline orientation for the grain was checked by selected-area electron diffraction (SAED).

Band Structure Calculations: The bulk spin polarization of $(\text{Mn}_{1-x}\text{Ni}_x)_{65}\text{Ga}_{35}$ with $x = 0.5$ was calculated by means of the CASPT code based on a pseudopotential method with a plane-wave basis set.^[39] The exchange and correlation effects were treated using the generalized gradient approximation (GGA).^[40] For all cases, an energy cut-off of 400 eV for the plane-wave expansion and a Monkhorst–Pack special k-point mesh of $12 \times 12 \times 12$ were used for Brillouin zone integrations. The convergence tolerance for the calculations was selected as a difference in total energy within 1×10^{-6} eV atom⁻¹.

Supporting Information

Supporting Information is available from the Wiley Online Library or from the author.

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- [1] S. Mülbauer, B. Binz, F. Jonietz, C. Pfleiderer, A. Rosch, A. Neubauer, R. Georgii, P. Boni, *Science* **2009**, *323*, 915.
 [2] A. Neubauer, C. Pfleiderer, B. Binz, A. Rosch, R. Ritz, P. G. Niklowitz, P. Boni, *Phys. Rev. Lett.* **2009**, *102*, 186602.
 [3] C. Pappas, E. Lelivre-Berna, P. Falus, P. M. Bentley, E. Moskvina, S. Grigoriev, P. Fouquet, B. Farago, *Phys. Rev. Lett.* **2009**, *102*, 197202.

- [4] A. Tonomura, X. Z. Yu, K. Yanagisawa, T. Matsuda, Y. Onose, N. Kanazawa, H. S. Park, Y. Tokura, *Nano Lett.* **2012**, *12*, 1673.
 [5] X. Z. Yu, N. Kanazawa, Y. Onose, K. Kimoto, W. Z. Zhang, S. Ishiwata, Y. Matsui, Y. Tokura, *Nat. Mater.* **2011**, *10*, 106.
 [6] H. Wilhelm, M. Baenitz, M. Schmidt, U. K. Rößler, A. A. Leonov, A. N. Bogdanov, *Phys. Rev. Lett.* **2011**, *107*, 127203.
 [7] X. Z. Yu, Y. Onose, N. Kanazawa, J. H. Park, J. H. Han, Y. Matsui, N. Nagaosa, Y. Tokura, *Nature* **2010**, *465*, 901.
 [8] S. Seki, X. Z. Yu, S. Ishiwata, Y. Tokura, *Science* **2012**, *336*, 198.
 [9] T. Adams, A. Chacon, M. Wagner, A. Bauer, G. Brandl, B. Pedersen, H. Berger, P. Lemmens, C. Pfleiderer, *Phys. Rev. Lett.* **2012**, *108*, 237204.
 [10] S. Seki, S. Ishiwata, Y. Tokura, *Phys. Rev. B* **2012**, *86*, 060403.
 [11] Y. Tokunaga, X. Z. Yu, J. S. White, H. M. Rønnow, D. Morkawa, Y. Taguchi, Y. Tokura, *Nat. Commun.* **2015**, *6*, 7638.
 [12] I. Kézsmárki, S. Bordács, P. Milde, E. Neuber, L. M. Eng, J. S. White, H. M. Rønnow, C. D. Dewhurst, M. Mochizuki, K. Yanai, H. Nakamura, D. Ehlers, V. Tsurkan, A. Loidl, *Nat. Mater.* **2015**, *14*, 1116.
 [13] T. H. R. Skyrme, *Nucl. Phys.* **1962**, *31*, 556.
 [14] B. Binz, A. Vishwanath, *Physica B* **2008**, *403*, 1336.
 [15] Y. Onose, Y. Okamura, S. Seki, S. Ishiwata, Y. Tokura, *Phys. Rev. Lett.* **2012**, *109*, 037603.
 [16] M. Mochizuki, X. Z. Yu, S. Seki, N. Kanazawa, W. Koshibae, J. Zang, M. Mostovoy, Y. Tokura, N. Nagaosa, *Nat. Mater.* **2014**, *13*, 241.
 [17] F. Jonietz, S. Mühlbauer, C. Pfleiderer, A. Neubauer, W. Münzer, A. Bauer, T. Adams, R. Georgii, P. Böni, R. A. Duine, K. Everschor, M. Garst, A. Rosch, *Science* **2010**, *330*, 1648.
 [18] T. Schulz, R. Ritz, A. Bauer, M. Halder, M. Wagner, C. Franz, C. Pfleiderer, K. Everschor, M. Garst, A. Rosch, *Nat. Phys.* **2012**, *8*, 301.
 [19] D. Liang, J. P. DeGrave, M. J. Stolt, Y. Tokura, S. Jin, *Nat. Commun.* **2015**, *6*, 8217.
 [20] S. S. P. Parkin, M. Hayashi, L. Thomas, *Science* **2008**, *320*, 190.
 [21] X. Z. Yu, M. Mostovoy, Y. Tokunaga, W. Z. Zhang, K. Kimoto, Y. Matsui, Y. Kaneko, N. Nagaosa, Y. Tokura, *Proc. Natl. Acad. Sci. USA* **2012**, *109*, 8856.
 [22] X. Z. Yu, Y. Tokunaga, Y. Kaneko, W. Z. Zhang, K. Kimoto, Y. Matsui, Y. Taguchi, Y. Tokura, *Nat. Commun.* **2014**, *5*, 3198.
 [23] S. Niziol, A. Bombik, W. Bazela, A. Szytula, D. Fruchart, *J. Magn. Magn. Mater.* **1982**, *27*, 181.
 [24] E. K. Liu, W. H. Wang, L. Feng, W. Zhu, G. J. Li, J. L. Chen, H. W. Zhang, G. H. Wu, C. B. Jiang, H. B. Xu, F. de Boer, *Nat. Commun.* **2012**, *3*, 873.
 [25] Y. Q. Li, E. K. Liu, G. H. Wu, W. H. Wang, Z. Y. Liu, *J. Appl. Phys.* **2014**, *116*, 223906.
 [26] H. Shiraishi, H. Niida, Y. Iguchi, S. Mitsudo, M. Motokawa, K. Ohayama, H. Miki, H. Onodera, T. Hori, K. Kanematsu, *J. Magn. Magn. Mater.* **1999**, *196*, 660.
 [27] N. Nagaosa, Y. Tokura, *Nat. Nanotechnol.* **2013**, *8*, 899.
 [28] K. Ueda, S. Iguchi, T. Suzuki, S. Ishiwata, Y. Taguchi, Y. Tokura, *Phys. Rev. Lett.* **2012**, *108*, 156601.
 [29] S. X. Huang, C. L. Chien, *Phys. Rev. Lett.* **2012**, *108*, 267201.
 [30] Y. Li, N. Kanazawa, X. Z. Yu, A. Tsukazaki, M. Kawasaki, M. Ichikawa, X. F. Jin, F. Kagawa, Y. Tokura, *Phys. Rev. Lett.* **2013**, *110*, 117202.
 [31] K. Kadowaki, K. Okuda, M. Date, *J. Phys. Soc. Jpn.* **1982**, *51*, 2433.
 [32] H. F. Du, J. P. DeGrave, F. Xue, D. Liang, W. Ning, J. Y. Yang, M. L. Tian, Y. H. Zhang, S. Jin, *Nano Lett.* **2014**, *14*, 2026.

- [33] N. Kanazawa, Y. Onose, T. Arima, D. Okuyama, K. Ohoyama, S. Wakimoto, K. Kakurai, S. Ishiwata, Y. Tokura, *Phys. Rev. Lett.* **2011**, *106*, 156603.
- [34] S. Heinze, K. von Bergmann, M. Menzel, J. Brede, A. Kubetzka, R. Wiesendanger, G. Bihlmayer, S. Blügel, *Nat. Phys.* **2011**, *7*, 713.
- [35] N. Romming, C. Hanneken, M. Menzel, J. E. Bickel, B. Wolter, K. von Bergmann, A. Kubetzka, R. Wiesendanger, *Science* **2013**, *341*, 636.
- [36] B. F. Miao, L. Sun, Y. W. Wu, X. D. Tao, X. Xiong, Y. Wen, R. X. Cao, P. Wang, D. Wu, Q. F. Zhan, B. You, J. Du, R. W. Li, H. F. Ding, *Phys. Rev. B* **2014**, *90*, 174411.
- [37] D. A. Gilbert, B. B. Maranville, A. L. Balk, B. J. Kirby, P. Fischer, D. T. Pierce, J. Unguris, J. A. Borchers, K. Liu, *Nat. Commun.* **2015**, *6*, 8462.
- [38] J. Li, A. Tan, K. W. Moon, A. Doran, M. A. Marcus, A. T. Young, E. Arenholz, S. Ma, R. F. Yang, C. Hwang, Z. Q. Qiu, *Nat. Commun.* **2014**, *5*, 4704.
- [39] M. Segall, P. J. Lindan, M. Probert, C. Pickard, P. Hasnip, S. Clark, M. Payne, *J. Phys.: Condens. Matter* **2002**, *14*, 2717.
- [40] E. Wimmer, H. Krakauer, M. Weinert, A. Freeman, *Phys. Rev. B* **1981**, *24*, 864.
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