

Interlayer-State-Coupling Dependent Ultrafast Charge Transfer in MoS₂/WS₂ Bilayers

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Light-induced interlayer ultrafast charge transfer in 2D heterostructures provides a new platform for optoelectronic and photovoltaic applications. The charge separation process is generally hypothesized to be dependent on the interlayer stackings and interactions, however, the quantitative characteristic and detailed mechanism remain elusive. Here, a systematical study on the interlayer charge transfer in model MoS₂/WS₂ bilayer system with variable stacking configurations by time-dependent density functional theory methods is demonstrated. The results show that the slight change of interlayer geometry can significantly modulate the charge transfer time from 100 fs to 1 ps scale. Detailed analysis further reveals that the transfer rate in MoS₂/WS₂ bilayers is governed by the electronic coupling between specific interlayer states, rather than the interlayer distances, and follows a universal dependence on the state-coupling strength. The results establish the interlayer stacking as an effective freedom to control ultrafast charge transfer dynamics in 2D heterostructures and facilitate their future applications in optoelectronics and light harvesting.

Since the discovery of graphene and the rise of MoS₂ as well as black phosphorus, atomically thin 2D crystals have grown

into a huge family of materials ranging from semimetal, semiconductors to insulators.^[1–11] Monolayer transition-metal dichalcogenides denoted as MX₂ (e.g., M = Mo, W, and X = S, Se, Te), have been prepared by physical exfoliation and chemical vapor deposition, providing more choices for 2D materials. The MX₂ materials share similar crystalline structures and symmetries, but possess distinct electronic properties in bandgaps, photoabsorption, and spin-orbit coupling strength.^[7–9] The heterostructures vertically reassembled from different 2D materials form even richer material systems, and thus provide a new platform for investigating new physics^[12–16] and exploring new applications.^[17–24] The heterostructures of two MX₂ are of particular interests because many of them form type II heterojunctions,^[25–27] which facilitate the efficient separation of photoexcited electrons and holes^[28,29] and therefore exhibit great potentials in the applications of photodetectors,^[30,31] photovoltaic cells,^[32,33] and light emitters.^[34]

The interlayer charge transfer in MX₂ heterostructures is of central importance in their photoresponse, which determines both the speed and efficiency of the charge separation.^[35,36] Since the charge transfer is mainly through the overlapping between interlayer electronic states, the charge transfer process is believed to be highly dependent on the interlayer stackings (twisting, translation, and spacing) and interactions. Femto-second pump-probe spectroscopy experiments reveals that the excited hole in MoS₂/WS₂ bilayer takes place in an ultrafast time scale.^[28] Wang et al. first report that collective motion of excitons at the interface leads to plasma oscillations associated with optical excitation in the ultrafast charge transfer in such van der Waals heterostructures, which provides a good insight in this new phenomenon.^[37] Although both experimental^[28,29] and theoretical efforts^[37,38] have been made to understand the ultrafast charge transfer process in MX₂ heterostructures, the quantitative characteristic and detailed mechanism for the interlayer stacking/interaction dependence still remain elusive.

Here we utilize the state-of-the-art time-dependent density functional theory method (TDDFT) and demonstrate a systematical study on the interlayer charge transfer in model MoS₂/WS₂ bilayer system with variable stacking configurations. Our results demonstrate that the interlayer twisting, translation, or

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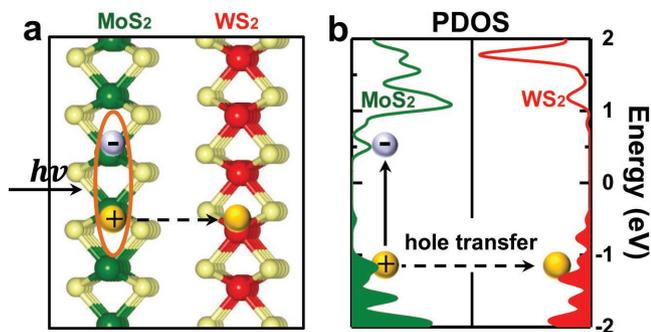


Figure 1. Atomic and electronic structure of the MoS₂/WS₂ bilayer. a) Side view of MoS₂/WS₂ bilayers. Green, red, and light yellow spheres represent Mo, W, and S atoms, respectively. b) Projected density of states (PDOS) on MoS₂ and WS₂ layer. Photoexcited holes will transfer from MoS₂ valence bands to WS₂.

spacing can significantly modulate interlayer charge transfer time from 100 to 1000 fs scale, a huge modulation that has not been realized before. Further analysis reveals that the transfer rate in MoS₂/WS₂ bilayers is governed by the coupling between specific interlayer states (rather than the total coupling strength) and follows a universal exponential dependence on their dipole coupling matrix values. This work establishes a firm correlation between charge transfer dynamics and interlayer stacking/interaction in 2D heterostructures on the atomic level, and thus facilitate their future applications in, for example, high speed optoelectronics and new generations of light harvesting.

The choice of MoS₂/WS₂ as a model system to study the interlayer charge transfer process in 2D heterostructures is mainly initiated by the ultrafast experiment from Wang and co-workers at UC Berkeley.^[28] MoS₂/WS₂ bilayers have a type II

band alignment: the conduction band minimum and valence band maximum at K point reside at MoS₂ and WS₂ layers, respectively [Figure 1; also see Figure S1 in the Supporting Information]. Since MoS₂ has an energy bandgap smaller than WS₂, we can selectively excite the MoS₂ by purposely choosing the excitation light with photon energy in between the bandgap of MoS₂ and WS₂. After photoexcitation, holes in MoS₂ will have the chance to transfer into the WS₂ because its valence band maximum is lower than that of WS₂; while the electrons will stay in MoS₂ since its conduction band minimum is also lower than WS₂ (Figure 1b).

MoS₂/WS₂ bilayers have many possible interlayer stacking configurations, i.e., AB₁-2H and AB₂-2H, AA₁-3R and AA₂-3R, and twisted ones.^[39,40] Here, we choose the most stable AB₁-2H as an example to show the time evolution of the interlayer charge transfer. In our calculations, we use Ehrenfest dynamics based on TDDFT approach to study excited-state dynamics, or ab initio TDDFT-molecular dynamics (MD) methods,^[41,42] which is widely proven reliable in describing quantum systems, such as optical absorption spectrum in dye-sensitized TiO₂ nanowire^[43] and electron injection and electron-hole recombination in dye solar cells.^[44] Optical transition in MoS₂/WS₂ bilayer is profoundly determined by the direct excitation of electron-hole pair in the individual layer since the interlayer interactions will only disturb the optical transition slightly.^[28] As shown in the band structure of MoS₂/WS₂ bilayer (Figure 2a), at K point in the first Brillouin zone the |−2> and |1> states are mainly distributed on MoS₂ while |−1> state is on WS₂. Since the |−2> and |−1> states at K point are located at two different layers (MoS₂ and WS₂, respectively), they are referred to as interlayer state. It should be noted that |−2> and |−1> states at K point are not sensitive to interlayer coupling, and they do not change much with the number of layers, while the states

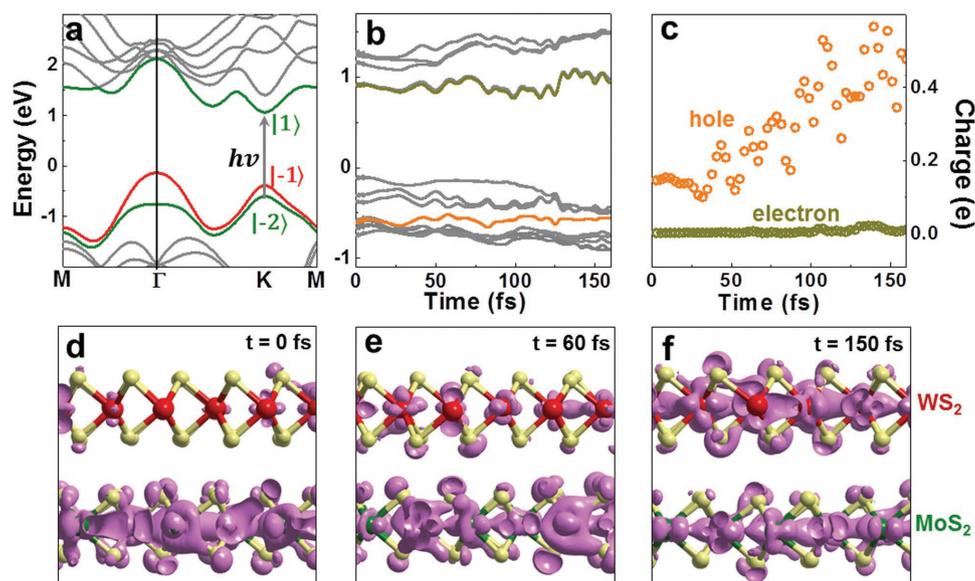


Figure 2. Charge transfer dynamics in AB₁-2H stacked MoS₂/WS₂ bilayers. a) Energy band dispersion of MoS₂/WS₂ bilayer in AB₁-2H stacking order. |1>, |−1>, and |−2> indicate these corresponding states at K point in the Brillouin zone. b) Evolution of electronic energy levels after photoexcitation. The orange (dark yellow) curve indicates the energy levels of photoexcited hole (electron) states. c) The fractions of photoexcited holes (electrons) that transferred from MoS₂ to WS₂ layer. d–f) Snapshots of the spatial distribution of hole density at 0, 60, and 150 fs after photoexcitation at a contour level of 0.02 e Å^{−3}. The upper (lower) layer is WS₂ (MoS₂).

at Γ point is quite allergic to the interlayer interactions. We note that direct interlayer excitation has a negligible strength as compared to intralayer excitation due to the minimal wavefunction overlap. Once this occurs, the interlayer exciton is formed right away upon excitation, and no charge transfer takes place in a short time <1 ps. By choosing the photon energy to be that of MoS_2 bandgap, it will mainly excite the electron from $|-2\rangle$ to $|1\rangle$ state and leaves the holes in MoS_2 layer. The holes will transfer into WS_2 layers afterward.

In the following, we look into the detailed hole transfer dynamics. We simulate the time evolution of interlayer charge transfer by simultaneously solving the time-dependent Kohn–Sham equation and the Newtonian motion of ions (ionic forces along the classical trajectory evaluated through the Ehrenfest theorem,^[41,42] see the Experimental Section for details). In Figure 2b, we show the evolution of Kohn–Sham energy levels of MoS_2/WS_2 bilayer. At the beginning, the energy of hole states (orange curve) is 0.48 eV below the valence band maximum. As the energy levels evolve in real time accompanied by the ionic motion, the hole states are getting closer to the valence band maximum. At $t = 150$ fs the difference becomes as small as 0.13 eV and the excited hole states in MoS_2 and original occupied states in WS_2 get largely mixed, or the hole transfer takes place. In Figure 2d–f, we give out the spatial distribution evolution of the hole states at different time. Immediately after photoexcitation, the holes are mostly distributed in MoS_2 ($<10\%$ of the states are in WS_2 , attributing to the weak interlayer state hybridization). At $t = 60$ fs, $\approx 25\%$ of the holes have transferred into WS_2 , and clearly at $t = 150$ fs, about 50% of the holes are localized in WS_2 . It means that the hole transfer between MoS_2 and WS_2 is taking place in an ultrafast way.

To gain quantitative information on charge transfer dynamics, we integrate the hole (electron) density (χ) on the WS_2 orbitals at different time after excitation (Figure 2c). Within 150 fs, about half of the holes density has transferred to WS_2 . While as expected the electrons still stay in MoS_2 and would not transfer to WS_2 during the whole simulation time. We note that an oscillation of about 30 fs is observed, possibly due to the ultrafast oscillation of electronic states (oscillation of ionic motion is of period much larger than 30 fs and thus can be excluded).^[37] The A_{1g} mode was found to be critical to the photoexcited hole dynamics. Here by doing Fourier transformation of dipole moment along the vertical direction of the heterojunction, we find that the A_{1g} phonon mode indeed plays an important role in the process of ultrafast hole transfer (see the Supporting Information for details). The formation of intralayer exciton prior to interlayer charge transfer and the collective motion of excitons is secondary for the dynamics of photoexcited charge, because the main driving force in such an ultrafast process is the specific state coupling as detailed below.

Now we turn to evaluate the dependence of charge transfer dynamics on interlayer stackings and interactions. There are five typical stacking configurations of AB_1 -2H, AB_2 -2H, AB_3 -2H, AA_1 -3R, and AA_2 -3R in MoS_2/WS_2 bilayers. For AB ones, the M–X bond directions in the two layers are opposite; while for AA ones, the directions are the same. So between AA and AB ones, the bilayers rotate by an angle of π ; and between AA_1 -3R (AB_1 -2H) and AA_2 -3R (AB_2 -2H), the two layers translate in-plane by 1.1 Å. From our calculations (Table 1) and also

Table 1. Calculated parameters for MoS_2/WS_2 bilayers.

Stacking		$d^a)$ [Å]	$E^b)$ [meV per atom]	$M^c)$ [e Å]	$\tau^d)$ [fs]
AB_1 -2H		6.3	−30.6	0.42	150
AB_1 -2H	Artificial	6.0	−27.5	0.62	120
AB_1 -2H	Artificial	7.0	−20.0	0.16	320
AB_1 -2H	Artificial	7.3	−16.2	0.005	1600
AB_2 -2H		6.3	−28.3	0.06	1100
AA_1 -3R		6.3	−28.7	0.02	1500
AA_2 -3R		6.8	−19.7	0.18	180

^{a)} d : interlayer spacing; ^{b)} E : formation energy; ^{c)} M : dipole transition matrix element; and ^{d)} τ : hole transfer lifetime.

previous results,^[22] AB_1 -2H, AB_2 -2H, and AA_1 -3R are the stable configurations with a smaller interlayer spacing of 6.3 Å; while AA_2 -3R is metastable with a larger interlayer spacing of 6.8 Å. The formation energies of AB_1 -2H, AB_2 -2H, and AA_1 -3R is of similar strength, but much lower than in AA_2 -3R.^[21] Both AA_2 -3R and AB_3 -2H share the similar orientation and interlayer distance (6.8 Å) and hole dynamics. Thus, the hole dynamics of AB_3 -2H stacking mode is presented for comparison in Figure S6 (Supporting Information). Since the charge transfer is related to the interlayer electronic coupling, naively one would expect that the shorter the interlayer distance is, the faster the interlayer charge transfer will be, or $\tau_{\text{AB}_1} \approx \tau_{\text{AB}_2} \approx \tau_{\text{AA}_1} \ll \tau_{\text{AA}_2}$.

In our results, we fit the time evolution data with an exponential equation $\chi = a + b \cdot \exp(-t/\tau)$, where τ is the charge transfer lifetime. As marked in Figure 3a–d, τ_{AB_1} or τ_{AA_2} is around 100 fs timescale and τ_{AB_2} or τ_{AA_1} is around 1000 fs scale (or $\tau_{\text{AB}_1} \approx \tau_{\text{AA}_2} \ll \tau_{\text{AB}_2} \approx \tau_{\text{AA}_1}$). It seems that the charge transfer time has no obvious correlation to interlayer coupling strength, which is quite counter-intuitive. The timescale is obtained by fitting to the simulated trends of ultrafast charge transfer upon photoexcitation. Direct simulation with trajectories longer than picoseconds is not only computationally unaffordable, but also blocked by the divergence of orbital propagation and break-down of mean field approach. We found that simulation in a relatively short timescale already gives a very reasonable fitting result of the charge transfer timescale (Figure S5, Supporting Information).

The above observed discrepancy between computation data and expectation drives us to rethink about the interlayer couplings. The usual mechanical or electronic interlayer coupling we talked about is actually the total one, which includes all the electronic states. However, the interlayer charge transfer takes place only between some specific interlayer states, and the charge transfer may be only related to the coupling between these specific ones. We therefore evaluate all the coupling elements between different specific interlayer states and eventually figure out the one that is responsible for the charge transfer dynamics, namely, the one between the $|-2\rangle$ and $|-1\rangle$ states at K point in the Brillouin zone. We use the dipole transition matrix element (M) to evaluate the coupling strength between the two states as

$$M = \langle -2 | \hat{Z} | -1 \rangle, \quad (1)$$

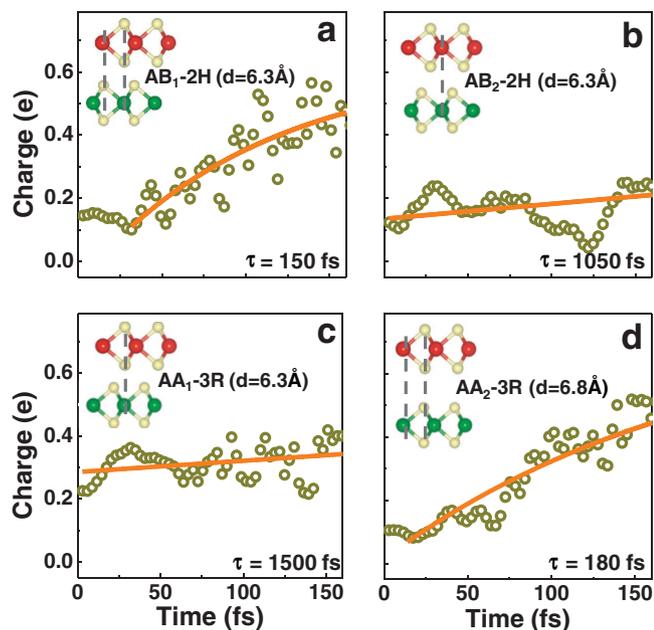


Figure 3. a–d) Hole transfer evolution for MoS₂/WS₂ in different stacking configurations. The transfer lifetime is fitted by an exponential relation. The insets give out the schematic atomic structure, interlayer spacing, and lifetime. From the consideration of total interlayer distances, one would expect $\tau_{AB1} \approx \tau_{AB2} \approx \tau_{AA1} \ll \tau_{AA2}$, but the simulation results show $\tau_{AB1} \approx \tau_{AA2} \ll \tau_{AB2} \approx \tau_{AA1}$. It reveals that the charger transfer time has no obvious correlation to the total interlayer coupling strength.

where \hat{Z} is the position operator along the vertical direction normal to the MX₂ plane. Quite interestingly, we found that $M_{AB1} > M_{AA2} \gg M_{AB2} > M_{AA1}$, which is positively correlated to $1/\tau$. Detailed analysis further revealed that $1/\tau$ is exponentially dependent on M , or $1/\tau \propto e^M$ (dashed line in Figure 4a).

In ref. [37], using both TDDFT and model Hamiltonian analysis Wang et al. studied dipole transition couplings between different layers in the heterojunctions and showed charge transfer time is dependent on stacking parameters. In the present work, the first principle simulations were further extended to different systems and longer times, where the charge transfer time is determined for every single stacking mode and thus the exponential dependence of charge transfer time on the interlayer-state-coupling strength can be plotted.

To further check whether this exponential dependence is universal in determining the interlayer charge transfer dynamics, we artificially tune the interlayer spacing from 6.0 to 7.3 Å in AB₁-2H stacking and obtained the τ and M (see Figure S2 in the Supporting Information for details). Again, all the data seat around the same $1/\tau$ versus e^M curve. So, the interlayer coupling between the $|-2\rangle$ and $|-1\rangle$ states is the universal factor that determines the charge transfer dynamics in MoS₂/WS₂ bilayers. To clarify why the specific coupling strength between $|-2\rangle$ and $|-1\rangle$ states at K point is crucial, we have checked all relative states (occupied or unoccupied states) and found only $M = \langle -2 | \hat{Z} | -1 \rangle$, is allergic to the photoexcited hole dynamics (with a typical value of 0.5 e Å for AB₁-2H stacking). The couplings between other pairs of states are much smaller (with a typical value of 10^{-3} e Å). The dependence of charge transfer

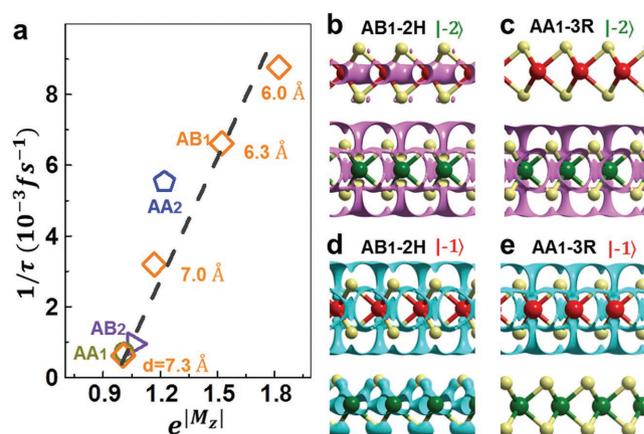


Figure 4. Interlayer-state-coupling dependent charge transfer rate in MoS₂/WS₂ bilayers. a) Dependence of the charge transfer rates ($1/\tau$) on the dipole transition coupling strength (M) between $|-2\rangle$ and $|-1\rangle$ states. AA₁-3R, AA₂-3R, AB₁-2H, and AB₂-2H data are, respectively, shown as circle, pentagon, square, and triangles. The interlayer spacing value of AB₁-2H (including those artificial ones) are labeled beside the data points. All data seat around the same curve, revealing a universal dependence of charge transfer rate on interlayer-state-coupling strength. b–e) Spatial distribution of $|-2\rangle$ and $|-1\rangle$ states in AB₁-2H and AA₁-3R stackings. The overlapping between $|-2\rangle$ and $|-1\rangle$ states along vertical direction on both the upper WS₂ and lower MoS₂ layers in AB₁-2H stacking is finite, while it is nearly zero in AA₁-3R stacking. Thus $M_{AB1} \gg M_{AA1}$ is understandable. The isosurface value is 1×10^{-3} e Å⁻³ in (b–e).

rate on the interlayer-state-coupling M justifies the importance of M as a measure for interface ultrafast dynamics.

Now we try to give out a physical picture why slight change of interlayer stacking configuration will give out dramatically different M . We use AB₁-2H and AA₁-3R bilayers as an example for illustration, which are both stable with the interlayer spacing of 6.3 Å. We directly draw the spatial distribution of $|-2\rangle$ (Figure 4b) and $|-1\rangle$ states (Figure 4d) in both WS₂ and MoS₂ layers. For AB₁-2H stacking, in the upper WS₂ layer, $|-2\rangle$ has finite overlapping with $|-1\rangle$ states along vertical direction and so as in the lower MoS₂ layer. In contrast, for AA₁-3R stacking, the overlapping in both layers is nearly zero. Since the \hat{Z} is an operation that projects electronic states to vertical directions, therefore $M_{AB1} \gg M_{AA1}$ is understandable (see Figure S3 in the Supporting Information for the other two stackings).

In the original experiment by Hong et al., the authors used film transfer method to prepare MoS₂/WS₂ bilayers, where the interlayer stacking configurations are not well controlled.^[28] Recently, MX₂ bilayers with defined interlayer geometry can be directly grown by chemical vapor deposition methods in several groups.^[15,20,21] And to utilize the two-color pump–probe optical technique, the charge transfer lifetime can be obtained by evaluating the rising up part of the pump–probe curve.^[28,29] Therefore, it is now the right time to experimentally study the charge transfer dynamics in MoS₂/WS₂ bilayers with different stackings predicted here.

In summary, we employ ab initio TDDFT-MD methods to investigate the ultrafast interlayer charge transfer dynamics in MoS₂/WS₂ bilayers. Our study reveals that slight interlayer geometry modulation of twisting, translation, or spacing can tune charge transfer dynamics very effectively, resulting in a

change of transfer lifetime spanning from 100 to 1000 fs time-scale. A universal exponential relationship between the charge transfer rate and the coupling strength between specific interlayer electronic states is established, based on detailed analysis of stacking-mode and layer-spacing modulation on the charge transfer dynamic processes. Based on these findings, one could utilize physical or chemical methods to control the interlayer geometry and therefore to control the charge transfer quantum dynamics, thus facilitating future applications of 2D heterostructures in novel optoelectronic and light harvesting devices.

Experimental Section

First principle calculations of MX_2 vertical heterostructures were performed using density functional theory implemented in the Vienna ab initio simulation package^[45] with Perdew, Burke, and Ernzerhof (PBE) generalized gradient approximation for the exchange–correlation functional.^[46,47] Because of the absence of strong chemical bonding between layers, van der Waals density functional in the opt88 form^[48] was employed for structural optimization. Both lattice constants and atomic positions were relaxed until all residual forces remain less than 10^{-2} eV \AA^{-1} and the total energy variation is less than 10^{-4} eV. The Brillouin zone was sampled by a set of $25 \times 25 \times 1$ k-mesh with an energy cutoff of 400 eV for plane waves. The thickness of vacuum layer was set to be larger than 15 \AA , so that interactions between repeated images are avoided. Formation energy (E) of the MoS_2/WS_2 heterostructure is defined as $E = (E_{\text{MoS}_2/\text{WS}_2} - E_{\text{MoS}_2} - E_{\text{WS}_2})/N$, where $E_{\text{MoS}_2/\text{WS}_2}$, E_{MoS_2} , E_{WS_2} are, respectively, the total energies of MoS_2/WS_2 bilayers, MoS_2 and WS_2 layers, and N is the number of atoms in the supercells.

The excited-state real-time TDDFT simulations were carried out with the time-dependent ab initio package TDAP^[42] based on SIESTA.^[49] Pseudopotentials of the Troullier–Martins type, the PBE exchange–correlation functional, and a local basis set of double- ζ polarized orbitals were used. It was noted that the band offset between the valence band maximum of WS_2 and MoS_2 in experiment (0.7 eV) were correctly reproduced by the PBE functional (0.5 eV).^[50] Although PBE functional usually underestimates the bandgaps, it is accurate enough to describe the spatial distribution of electronic states and the state couplings, which are crucial in the dynamic simulations.^[51] In addition, very similar band structures based on PBE functional and HSE06 functional are shown in Figure S7 (see the Supporting Information for details). Supercells in rectangle shape containing 108 atoms in the supercells were used to model bilayers with a single k-point for integration in the Brillouin zone and the states relative to the photoexcited states especially at K point in the first Brillouin zone were approximately folded to the supercells. The time step of all simulations was set to be 0.024 fs. Electron–hole interaction and electron–phonon effects were naturally included in the methods. The initial velocities of ions were assigned according to the equilibrium Boltzmann–Maxwell distribution at a given temperature of 350 K. It should be noted that some energy levels in the supercells were used may be degenerate, so states with similar energy and spatial distributions have been checked in the following dynamic simulations to ensure the reliability of the results.

Supporting Information

Supporting Information is available from the Wiley Online Library or from the author.

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Conflict of Interest

The authors declare no conflict of interest.

Keywords

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- [1] A. K. Geim, K. S. Novoselov, *Nat. Mater.* **2007**, *6*, 183.
- [2] A. Frenzel, C. Lui, Y. Shin, J. Kong, N. Gedik, *Phys. Rev. Lett.* **2014**, *113*, 056602.
- [3] A. Splendiani, L. Sun, Y. Zhang, T. Li, J. Kim, C.-Y. Chim, G. Galli, F. Wang, *Nano Lett.* **2010**, *10*, 1271.
- [4] K. F. Mak, C. Lee, J. Hone, J. Shan, T. F. Heinz, *Phys. Rev. Lett.* **2010**, *105*, 136805.
- [5] K. F. Mak, K. L. McGill, J. Park, P. L. McEuen, *Science* **2014**, *344*, 1489.
- [6] Z. Ye, T. Cao, K. O'Brien, H. Zhu, X. Yin, Y. Wang, S. G. Louie, X. Zhang, *Nature* **2014**, *513*, 214.
- [7] Q. H. Wang, K. Kalantar-Zadeh, A. Kis, J. N. Coleman, M. S. Strano, *Nat. Nanotechnol.* **2012**, *7*, 699.
- [8] F. Xia, H. Wang, D. Xiao, M. Dubey, A. Ramasubramaniam, *Nat. Photonics* **2014**, *8*, 899.
- [9] B. W. Baugher, H. O. Churchill, Y. Yang, P. Jarillo-Herrero, *Nat. Nanotechnol.* **2014**, *9*, 262.
- [10] H. Wang, C. Zhang, F. Rana, *Nano Lett.* **2015**, *15*, 339.
- [11] L. Li, Y. Yu, G. J. Ye, Q. Ge, X. Ou, H. Wu, D. Feng, X. H. Chen, Y. Zhang, *Nat. Nanotechnol.* **2014**, *9*, 372.
- [12] A. K. Geim, I. V. Grigorieva, *Nature* **2013**, *499*, 419.
- [13] B. Hunt, J. D. Sanchez-Yamagishi, A. F. Young, M. Yankowitz, B. J. LeRoy, K. Watanabe, T. Taniguchi, P. Moon, M. Koshino, P. Jarillo-Herrero, *Science* **2013**, *340*, 1427.
- [14] C. H. Lee, G. H. Lee, A. M. Van Der Zande, W. Chen, Y. Li, M. H. Han, M. X. Cui, G. Arefe, C. Nuckolls, T. F. Heinz, *Nat. Nanotechnol.* **2014**, *9*, 676.
- [15] Y. Gong, J. Lin, X. Wang, G. Shi, S. Lei, Z. Lin, X. Zou, G. Ye, R. Vajtai, B. I. Yakobson, *Nat. Mater.* **2014**, *13*, 1135.
- [16] M.-H. Chiu, C. Zhang, H.-W. Shiu, C.-P. Chuu, C.-H. Chen, C.-Y. S. Chang, C.-H. Chen, M.-Y. Chou, C.-K. Shih, L.-J. Li, *Nat. Commun.* **2015**, *6*, 7666.
- [17] H. Heo, J. H. Sung, S. Cha, B.-G. Jang, J.-Y. Kim, G. Jin, D. Lee, J.-H. Ahn, M.-J. Lee, J. H. Shim, *Nat. Commun.* **2015**, *6*, 7372.
- [18] A. F. Rigosi, H. M. Hill, Y. Li, A. Chernikov, T. F. Heinz, *Nano Lett.* **2015**, *15*, 5033.
- [19] P. Rivera, J. R. Schaibley, A. M. Jones, J. S. Ross, S. Wu, G. Aivazian, P. Klement, K. Seyler, G. Clark, N. J. Ghimire, *Nat. Commun.* **2015**, *6*, 6242.
- [20] Q. Zhang, X. Xiao, R. Zhao, D. Lv, G. Xu, Z. Lu, L. Sun, S. Lin, X. Gao, J. Zhou, *Angew. Chem., Int. Ed.* **2015**, *54*, 8957.

- [21] J. Zhang, J. Wang, P. Chen, Y. Sun, S. Wu, Z. Jia, X. Lu, H. Yu, W. Chen, J. Zhu, *Adv. Mater.* **2016**, *28*, 1950.
- [22] S. Han, H. Kwon, S. K. Kim, S. Ryu, W. S. Yun, D. Kim, J. Hwang, J.-S. Kang, J. Baik, H. Shin, *Phys. Rev. B* **2011**, *84*, 045409.
- [23] L. Zhang, A. Zunger, *Nano Lett.* **2015**, *15*, 949.
- [24] J. Kang, L. Zhang, S. H. Wei, *J. Phys. Chem. Lett.* **2016**, *7*, 597.
- [25] D. Meier, T. Kuschel, L. Shen, A. Gupta, T. Kikkawa, K.-I. Uchida, E. Saitoh, J.-M. Schmalhorst, G. Reiss, *Phys. Rev. B* **2013**, *87*, 054421.
- [26] J. Kang, S. Tongay, J. Zhou, J. Li, J. Wu, *Appl. Phys. Lett.* **2013**, *102*, 012111.
- [27] C. Gong, H. Zhang, W. Wang, L. Colombo, R. M. Wallace, K. Cho, *Appl. Phys. Lett.* **2013**, *103*, 053513.
- [28] X. Hong, J. Kim, S.-F. Shi, Y. Zhang, C. Jin, Y. Sun, S. Tongay, J. Wu, Y. Zhang, F. Wang, *Nat. Nanotechnol.* **2014**, *9*, 682.
- [29] F. Ceballos, M. Z. Bellus, H.-Y. Chiu, H. Zhao, *ACS Nano* **2014**, *8*, 12717.
- [30] L. Britnell, R. Ribeiro, A. Eckmann, R. Jalil, B. Belle, A. Mishchenko, Y.-J. Kim, R. Gorbachev, T. Georgiou, S. Morozov, *Science* **2013**, *340*, 1311.
- [31] W. J. Yu, Y. Liu, H. Zhou, A. Yin, Z. Li, Y. Huang, X. Duan, *Nat. Nanotechnol.* **2013**, *8*, 952.
- [32] M. Bernardi, M. Palumbo, J. C. Grossman, *Nano Lett.* **2013**, *13*, 3664.
- [33] Y. Yu, S. Hu, L. Su, L. Huang, Y. Liu, Z. Jin, A. A. Purezky, D. B. Geohegan, K. W. Kim, Y. Zhang, *Nano Lett.* **2014**, *15*, 486.
- [34] J. S. Ross, P. Klement, A. M. Jones, N. J. Ghimire, J. Yan, D. Mandrus, T. Taniguchi, K. Watanabe, K. Kitamura, W. Yao, *Nat. Nanotechnol.* **2014**, *9*, 268.
- [35] S. M. Falke, C. A. Rozzi, D. Brida, M. Maiuri, M. Amato, E. Sommer, A. De Sio, A. Rubio, G. Cerullo, E. Molinari, *Science* **2014**, *344*, 1001.
- [36] C. A. Rozzi, S. M. Falke, N. Spallanzani, A. Rubio, E. Molinari, D. Brida, M. Maiuri, G. Cerullo, H. Schramm, J. Christoffers, *Nat. Commun.* **2013**, *4*, 1602.
- [37] H. Wang, J. Bang, Y. Sun, L. Liang, D. West, V. Meunier, S. Zhang, *Nat. Commun.* **2016**, *7*, 11504.
- [38] R. Long, O. V. Prezhdo, *Nano Lett.* **2016**, *16*, 1996.
- [39] A. M. van Der Zande, J. Kunstmann, A. Chernikov, D. A. Chenet, Y. You, X. Zhang, P. Y. Huang, T. C. Berkelbach, L. Wang, F. Zhang, *Nano Lett.* **2014**, *14*, 3869.
- [40] K. Liu, L. Zhang, T. Cao, C. Jin, D. Qiu, Q. Zhou, A. Zettl, P. Yang, S. G. Louie, F. Wang, *Nat. Commun.* **2014**, *5*, 4966.
- [41] E. Runge, E. K. Gross, *Phys. Rev. Lett.* **1984**, *52*, 997.
- [42] S. Meng, E. Kaxiras, *J. Chem. Phys.* **2008**, *129*, 054110.
- [43] S. Meng, J. Ren, E. Kaxiras, *Nano Lett.* **2008**, *8*, 3266.
- [44] S. Meng, E. Kaxiras, *Nano Lett.* **2010**, *10*, 1238.
- [45] G. Kresse, J. Furthmüller, *Comput. Mater. Sci.* **1996**, *6*, 15.
- [46] P. E. Blöchl, *Phys. Rev. B* **1994**, *50*, 17953.
- [47] J. P. Perdew, K. Burke, M. Ernzerhof, *Phys. Rev. Lett.* **1996**, *77*, 3865.
- [48] J. Klimeš, D. R. Bowler, A. Michaelides, *Phys. Rev. B* **2011**, *83*, 195131.
- [49] J. M. Soler, E. Artacho, J. D. Gale, A. García, J. Junquera, P. Ordejón, D. J. Sánchez-Portal, *J. Phys.: Condens. Matter.* **2002**, *14*, 2745.
- [50] H. M. Hill, A. F. Rigosi, K. T. Rim, G. W. Flynn, T. F. Heinz, *Nano Lett.* **2016**, *16*, 4831.
- [51] W. Ma, J. Zhang, L. Yan, Y. Jiao, Y. Gao, S. Meng, *Comput. Mater. Sci.* **2016**, *112*, 478.